

# Askern Moss Road Infant Academy and Askern Littlemoor Infant Academy



| VERSION | AUTHOR  | SUMMARY OF CHANGES                       | DATE PUBLISHED | DATE OF REVIEW |
|---------|---------|------------------------------------------|----------------|----------------|
| 1.0     | CL      | New Policy                               | March 2025     | March 2026     |
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|         |         |                                          |                |                |

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## **Aims of this Policy**

The aim of this policy is to ensure that all children leave our school with a secure understanding of the four operations and can confidently use both written and mental calculation strategies in a range of contexts.

It also aims to ensure that consistent strategies, models and images are used across the school to embed and deepen children's learning and understanding of mathematical concepts.

## **How This Policy Should Be Used**

This policy has been designed to support the teaching and planning of mathematics in our school. It outlines key strategies; however, teachers must plan opportunities for pupils to apply these through the White Rose small steps for learning, for example when solving problems or when opportunities arise across the wider curriculum.

The examples and illustrations included are not exhaustive but provide an overall picture of what mathematics in our school should look like. This document is not a scheme of work and must be used alongside our school maths policy and curriculum documents.

The White Rose Maths schemes of learning should be used to plan small steps in learning, alongside mastery guidance from NCETM and this calculation policy.

## **The CPA Approach**

This policy sets out the progression of strategies and written methods that children will be taught as they develop their understanding of the four operations. Strategies are structured using the Concrete, Pictorial, Abstract (CPA) approach to develop deep understanding and mastery of mathematical concepts.

Children begin by using concrete objects to make sense of a concept or problem. These may include real-life objects such as fruit, or mathematical resources such as straws, counters or cubes. Learning then develops through the use of images, models and pupils' own pictorial representations before moving on to abstract mathematics.

Children will move along this continuum repeatedly, revisiting earlier stages as concepts are extended. It is important to note that movement through the CPA stages is not linear. For example, children who are working at a pictorial or abstract level may still benefit from the use of concrete resources to support reasoning, explanation and understanding.

Children must be supported to develop depth within each strategy through the CPA approach and should not learn methods purely as procedures.

## Use of Manipulatives to Support Learning

Manipulatives are a key part of high-quality mathematics teaching and are used to support all pupils in accessing, understanding and engaging with mathematical concepts. Concrete resources such as counters, cubes, number lines, bead strings and other practical apparatus enable children to explore mathematical ideas in a hands-on way. They help to make abstract concepts visible and support the development of deep, secure understanding.

Teachers should carefully select and use manipulatives to match the mathematical concept being taught, ensuring a clear link between the concrete, pictorial and abstract representations. Pupils should be encouraged to independently choose and use manipulatives where appropriate, developing autonomy and confidence in their learning.

Consistent use of agreed manipulatives across the school supports progression, coherence and familiarity, enabling children to build on prior knowledge and make connections within their learning.

## Progression and Use of Calculation Strategies

Although strategies are taught in a progressive sequence, they are intended to equip children with a 'toolbox' of skills that can be applied in a range of contexts. As new strategies are introduced, they do not replace previous learning but build upon it, allowing children to select from a range of approaches.

As pupils become more independent, they should be encouraged to choose the most efficient strategy for the task. Developing this independence is a key aim of mathematics teaching.

For clarity, strategies are organised into the four operations. However, addition and subtraction, and multiplication and division, should be taught alongside one another to support connections and relationships within mathematics. For example, counting on (addition) should be taught alongside counting back (subtraction).

Children should progress through strategies at a pace appropriate to their age-related expectations, as defined by the EYFS framework and National Curriculum. Effective teaching relies on the development of strong number sense, fluency and the ability to reason mathematically.

## Importance of Vocabulary

The White Rose Maths scheme places strong emphasis on the use of precise mathematical language as a central part of learning. Without the appropriate vocabulary, children are unable to clearly explain and justify their mathematical thinking.

New vocabulary should be introduced in meaningful contexts, using appropriate concrete resources, images or diagrams, and should be explicitly taught. Teachers must model correct mathematical language and maintain high expectations, only accepting accurate terminology.

| Correct Vocabulary         | Incorrect Vocabulary |
|----------------------------|----------------------|
| Ones                       | Units                |
| Is equal to                | Equals               |
| Zero                       | Oh ( o )             |
| Number sentence / Equation | Sum (s)              |
|                            |                      |

## Mathematical Language

|                       | Foundation Stage                                                                                                                                                            | Year 1                                                                                                                                                                                                                                                                                                                                                                                                                                               | Year 2                                                                                                                                                                                                                                                       |
|-----------------------|-----------------------------------------------------------------------------------------------------------------------------------------------------------------------------|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|--------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| <b>Addition</b>       | add, more, and, make, sum, total, altogether, score, double, one more, two more, ten more..., how many more to make... ?, how many more is... than...?                      | number bonds, add, more, plus, make, sum, total, altogether, inverse double, near double, equals, is the same as (including equals sign), score, one more, two more... ten more, how many more to make...?, how many more is... than...?, how much more is...?                                                                                                                                                                                       | add, addition, more, plus, make, sum, total, altogether, score, double, near double, one more, two more... ten more... one hundred more, how many more to make...?, how many more is... than...?, how much more is...?, tens boundary                        |
| <b>Subtraction</b>    | take (away), leave, how many are left/left over?, how many have gone?, one less, two less... ten less..., how many fewer is... than...?, difference between, is the same as | How many ... were there first? How many were taken away? How many are there now? Subtract, take away, minus, leave, how many fewer is...than..?, how much less is...? half, halve, how many are left/left over?, how many are gone?, one less, two less, ten less..., how many fewer is... than...?, how much less is...? =, equals, sign, is the same as, count on, count back, difference between. how many more is...than..?, how much more is..? | subtract, minus, leave, how many are left/left over?, how many less is... than...?, how much fewer is...?, difference between, half, halve, equals, sign, is the same as, partition, inverse, count on , count back, one less, ten less... one hundred less. |
| <b>Multiplication</b> | group, lots of, double                                                                                                                                                      | odd, even, count in twos, fives, count in tens (forwards from/backwards from), how many times? lots of, groups of, once, twice, five times, ten times , multiple of, times, multiply, multiply by, array, row, column, double.                                                                                                                                                                                                                       | odd, even, twos, fives, tens, threes, lots of, groups of, once, twice, three times, five times, ten times, multiple of, times, multiply, multiply by, repeated addition, array, row, column, double.                                                         |
| <b>Division</b>       |                                                                                                                                                                             | halve, share, share equally, groups, equal groups of, divide, divided by, left, left over                                                                                                                                                                                                                                                                                                                                                            | groups of, equal groups of, halve, share, share equally, divide, divided by, divided into, repeated subtraction, inverse.                                                                                                                                    |

### End of Year Expectations

| EYFS                                                                           | Year 1                    | Year 2                           |
|--------------------------------------------------------------------------------|---------------------------|----------------------------------|
| <ul style="list-style-type: none"> <li>Have a deep understanding of</li> </ul> | read, write and interpret | solve problems with addition and |

|                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           |
|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| <p>number to 10, including the composition of each number.</p> <ul style="list-style-type: none"> <li>• Subitise (recognise quantities without counting) up to 5.</li> <li>• Automatically recall (without reference to rhymes, counting or other aids) number bonds up to 5 (including subtraction facts) and some number bonds to 10, including double facts.</li> <li>• Verbally count beyond 20, recognising the pattern of the counting system.</li> <li>• Compare quantities up to 10 in different contexts, recognising when one quantity is greater than, less than or the same as the other quantity.</li> <li>• Explore and represent patterns within numbers up to 10, including evens and odds, double facts and how quantities can be distributed equally.</li> </ul> | <p>mathematical statements involving addition (+), subtraction (−) and equals (=) signs</p> <ul style="list-style-type: none"> <li>• represent and use number bonds and related subtraction facts within 20</li> <li>• add and subtract one-digit and two-digit numbers to 20, including zero</li> <li>• solve one-step problems that involve addition and subtraction, using concrete objects and pictorial representations, and missing number problems such as <math>7 = ? - 9</math>.</li> <li>• solve one-step problems involving multiplication and division, by calculating the answer using concrete objects</li> <li>• solve one-step problems involving multiplication and division using pictorial representations and arrays with</li> </ul> | <p>subtraction:</p> <ul style="list-style-type: none"> <li>• using concrete objects and pictorial representations, including those involving numbers, quantities and measures</li> <li>• applying their increasing knowledge of mental and written methods <ul style="list-style-type: none"> <li>• recall and use addition and subtraction facts to 20 fluently</li> <li>• derive and use related facts up to 100</li> <li>• add and subtract numbers using concrete objects, pictorial representations, and mentally, including: <ul style="list-style-type: none"> <li>o a two-digit number and ones</li> <li>o a two-digit number and tens</li> <li>o two two-digit numbers</li> <li>o adding three one-digit numbers</li> </ul> </li> <li>• show that addition of two numbers can be done in any order (commutative) and subtraction of one number from another cannot</li> <li>• recognise and use the inverse relationship between addition and subtraction and use this to check calculations and solve missing number problems</li> <li>• recall and use multiplication and division facts for the 2, 5 and 10 multiplication tables, including recognising odd and even numbers</li> <li>• calculate mathematical statements for multiplication and division within the multiplication tables and write them using the multiplication (<math>\times</math>), division (<math>\div</math>) and equals (=) signs</li> <li>• show that multiplication of two numbers can be done in any order (commutative) and division of one number by another cannot</li> <li>• solve problems involving multiplication and division, using materials, arrays, repeated addition, mental methods, and multiplication and division facts, including problems in contexts</li> </ul> </li> </ul> |
|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|

## Mathematics in the EYFS

The objective for those working in Early Years is to ensure that all children develop firm mathematical foundations in a way that is engaging and appropriate for their age.

There are six main areas that collectively underpin children's early mathematical learning, and which provide the firm foundations for the maths that children will encounter as they go up the years in primary school.

They are:

### Cardinality and Counting:

The cardinal value of a number refers to the quantity of things it represents, e.g. the numerosity, 'howmanyness', or 'threeness' of three. When children understand the cardinality of numbers, they know what the numbers mean in terms of knowing how many things they refer to. Counting is one way of establishing how many things are in a group, because the last number you say tells you how many there are. Children enjoy learning the sequence of counting numbers long before they understand the cardinal values of the numbers. Subitising is another way of recognising how many there are, without counting.

### Comparison:

Comparing numbers involves knowing which numbers are worth more or less than each other. This depends both on understanding cardinal values of numbers and also knowing that the later counting numbers are worth more (because the next number is always one more). This understanding underpins the mental number line which children will develop later, which represents the relative value of numbers, i.e how much bigger or smaller they are than each other.

### Composition:

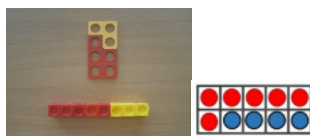
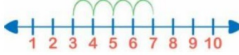
Knowing numbers are made up of two or more other smaller numbers involves 'part-whole' understanding. Learning to 'see' a whole number and its parts at the same time is a key development in children's number understanding. Partitioning numbers into other numbers and putting them back together again underpins understanding of addition and subtraction as inverse operations.

### Pattern:

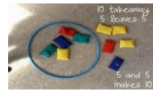
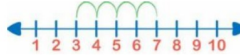
Seeking and exploring patterns is at the heart of mathematics (Schoenfeld, 1992). Developing an awareness of pattern helps young children to notice and understand mathematical relationships. Clements and Sarama (2007) identify that patterns may provide the foundations of algebraic thinking, since they provide the opportunity for young children to observe and verbalise generalisations.

The focus in this section is on repeating patterns, progressing from children copying simple alternating AB patterns to identifying different structures in the 'unit of repeat', such as ABB or ABBC. Patterns can be made with objects like coloured cubes, small toys, buttons and keys, and with outdoor materials like pine cones, leaves or large blocks, as well as with movements and sounds, linking with music, dance, phonics and rhymes. Children can also spot and create patterns in a range of other contexts, such as printed patterns, timetables, numbers and stories.

## Addition

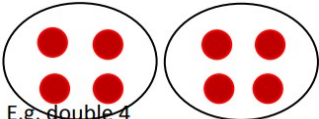
| Concrete                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                | Pictorial                                                                                                                                                                                                                                                                                                               | Abstract |   |   |   |   |   |                                                                                                                                                                                                                                                                             |
|-----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|----------|---|---|---|---|---|-----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| <p>Children are encouraged to gain a sense of the number system through the use of counting concrete objects.</p> <p>They <b>combine 2 groups</b> in practical ways using counters, cubes, numicon and ten frames.</p> <div></div> <div></div> <p>They also understand addition as <b>counting on</b> and will count on in using objects, cubes and beadstring.</p> <div></div> <p>They will show <b>number bonds to 10</b> using numicon and ten frame.</p> <div></div> <p>They will find <b>one more</b> than by singing counting songs, counting items, using numicon and using 5 and ten frames. They will be encouraged to see the link between counting forwards and the one more number.</p> <div></div> | <p>Children will learn to count on using a number line.</p> <div></div> <p>Place number cards in order and say which is one more.</p> <div><table><tr><td>1</td><td>2</td><td>3</td><td>4</td><td>5</td><td>6</td></tr></table></div> | 1        | 2 | 3 | 4 | 5 | 6 | <p>They begin to use + and = They are encouraged to develop a mental picture of the number system in their heads to use for calculations. Higher attaining children may be able to represent their calculations using symbols and numbers within a written calculation.</p> |
| 1                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       | 2                                                                                                                                                                                                                                                                                                                       | 3        | 4 | 5 | 6 |   |   |                                                                                                                                                                                                                                                                             |

## Subtraction

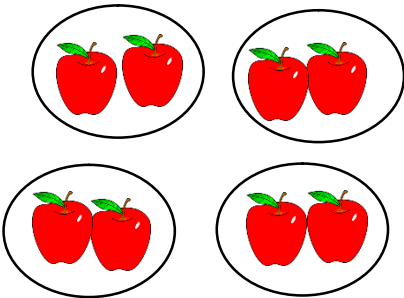
| Concrete                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           | Pictorial                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               | Abstract |   |   |   |   |   |                                                                                                                                                                                                                                                                             |
|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|----------|---|---|---|---|---|-----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| <div></div> <p>Children are encouraged to gain a sense of the number system through the use of counting concrete objects. They begin to 'take-away' using objects, counters, cubes and beadstring.</p> <div></div> <p>Children will also show this on a ten frame.</p> <p>They will find <b>one less</b> than by singing counting songs, counting items, using numicon and using 5 and ten frames.</p> <p>They will be encouraged to see the link between</p> <div></div> | <div></div> <p>Children will learn to count back using a number line.</p> <p>They will also begin to record subtraction by 'crossing out' counters on a ten frame.</p> <div></div> <p>Place number cards in order and say which is one less.</p> <div><table><tr><td>1</td><td>2</td><td>3</td><td>4</td><td>5</td><td>6</td></tr></table></div> | 1        | 2 | 3 | 4 | 5 | 6 | <p>They begin to use - and = They are encouraged to develop a mental picture of the number system in their heads to use for calculations. Higher attaining children may be able to represent their calculations using symbols and numbers within a written calculation.</p> |
| 1                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  | 2                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       | 3        | 4 | 5 | 6 |   |   |                                                                                                                                                                                                                                                                             |

counting forwards and the one more number.

## Multiplication (Doubling)

| Concrete                                                                                                                                                   | Pictorial                                                                                                                                                     | Abstract |
|------------------------------------------------------------------------------------------------------------------------------------------------------------|---------------------------------------------------------------------------------------------------------------------------------------------------------------|----------|
| <p>Use counting equipment alongside numicon to get double an amount.</p>  | <p>Draw counters with same amount in both circles,</p>  <p>E.g. double 4</p> |          |

## Division (Sharing and Grouping)

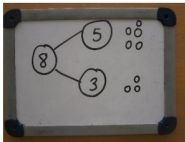
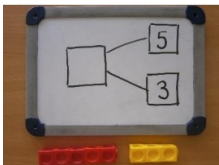
| Concrete                                                                                                                                                                                                                                                                                                                                                                                                     | Pictorial                                                                                                                                                                                    | Abstract |
|--------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|----------|
| <p>Use counting equipment to <b>share</b> an even number of items between people or teddies for example. Count out one at a time to make sure each group is equal.</p> <p>E.g. "How can I share six animals between two monkeys?"</p>  <p>Children will be asked to make <b>groups</b> using the small world animals.</p> | <p>Draw pictures to show how they have shared between groups. E.g. 8 apples shared between 4 people:</p>  |          |

## Add with numbers up to 20

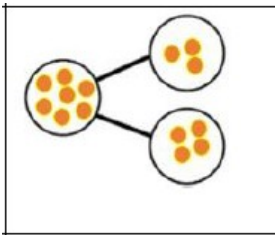
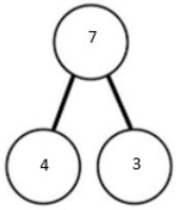
### Key number skills for addition at Year 1:

- Read and write numbers to 100 forwards and backwards, from any given number.
- Read and write numbers from 1 – 20 in numerals and words.
- Recall bonds to 10 and 20 and addition facts within 20.
- Count to and across 100.
- Count in multiples of 1, 2, 5 and 10.
- Solve simple one step problems involving addition using objects, number lines and pictorial representations

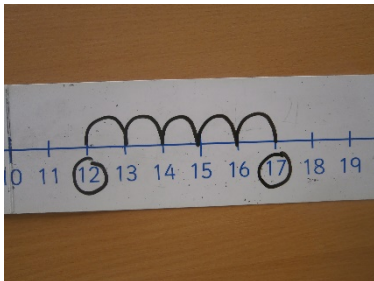
### Number Bonds to 10

| Concrete                                                                                                                                                                                                                                                                                                                                                                                  | Pictorial                                                                                                                                                                                                                                                                                      | Abstract                                                                                                                                                                                                                                                         |
|-------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| <p>Begin with numbers to 10 ensuring the children are secure with these. Use numicon and bucket balance to show equivalence of numbers.</p>  <p>Use counting equipment such as cubes to add two parts together.</p>  | <p>Jottings to show workings out with 2 numbers being added together. Part-part-whole model with numbers given for children to draw.</p>  <p>Use ten frames (and numbers up to 10) to show number bonds.</p> | <p>Record as addition sentences: <math>3 + 5 = 8</math> <math>5 + 3 = 8</math> <math>8 = 3 + 5</math> <math>8 = 5 + 3</math> Part-part-whole model with total missing.</p>  |

### Combining two parts to make a whole

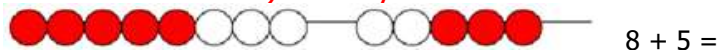
| Concrete                                                                            | Pictorial                                                                                                                                                                                             | Abstract                                                                                                                                                                |
|-------------------------------------------------------------------------------------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
|  | <p>Children to represent the cubes using dots or crosses. They could put each part on a part whole model too.</p>  | <p><math>4 + 3 = 7</math> Four is a part, 3 is a part and the whole is seven.</p>  |

## Counting on using a number line.

| Concrete                                                                                                                                                                                                    | Pictorial                                                                                                                                                                                                    | Abstract                                                                                                       |
|-------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|--------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|----------------------------------------------------------------------------------------------------------------|
|  <p>Start with the larger number on the bead string and then count on to the smaller number 1 by 1 to find the answer.</p> | $12 + 5 = 17$  <p>Start at the larger number on the number line and count on in ones or in one jump to find the answer.</p> | $12 + 5 = 17$ <p>Place the larger number in your head and count on the smaller number to find your answer.</p> |

### Note:

This builds on from prior learning of adding by combining two sets of objects into one group (5 cubes and 3 cubes) in Early Years.



### Children Should:

- Have access to a wide range of counting equipment, everyday objects, number tracks and number lines and be shown numbers in different contexts
- Understand that addition can be done in any order
- Read and write the addition (+) and equals (=) signs within number sentences
- Strengthen their understanding of the = sign
- Interpret addition number sentences and solve missing box problems, using concrete objects and number lines

## Year 2

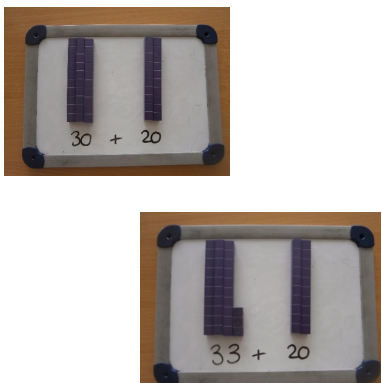
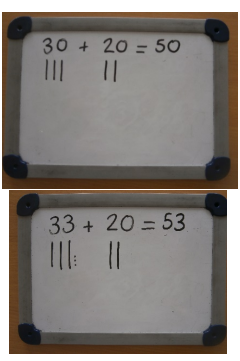
### Add numbers with up to 2-digits

#### Key number skills for addition at Year 2:

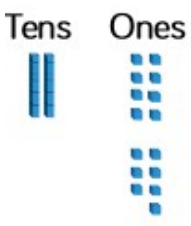
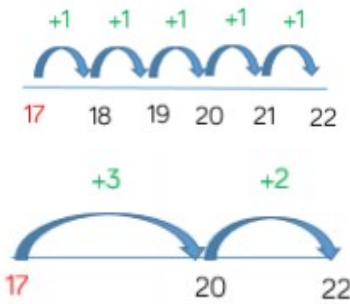
- Add a 2-digit number and ones (e.g.  $27 + 6$ ).
- Add a 2-digit number and tens (e.g.  $23 + 40$ ).
- Add pairs of 2-digit numbers which bridge ten (e.g.  $35 + 47$ ).
- Add three single digit numbers ( $5 + 9 + 7$ ).
- Show that adding can be done in any order (the commutative law).
- Recall bonds to 20 and bonds of tens to 100.
- Count in steps of 2, 3 and 5 and count in tens from any number.
- Solve problems with addition, using concrete objects, pictorial representations, involving numbers, quantities and measures and applying mental and written methods.

*Note: Continue to refer to the part-whole model and bar model to record addition and to support the commutative law.*

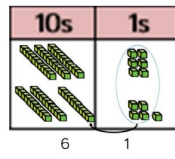
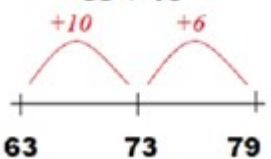
## Adding a 2-digit number and tens

| Concrete                                                                                                                                                | Pictorial                                                                                                                                                                                                                                         | Abstract                                                                                                                                                                                                                                                                                                                                                                                                      |      |      |  |    |  |  |  |  |
|---------------------------------------------------------------------------------------------------------------------------------------------------------|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|------|------|--|----|--|--|--|--|
| <p>Use base ten sticks to add the two multiples of tens together.</p>  | <p>When adding two multiples of ten, draw sticks to represent the base ten. When adding a 2digit and multiple of ten, draw the base ten as sticks and dots.</p>  | <p>Use place value charts alongside in preparation for column addition. 23 + 40.</p> <table data-bbox="1083 389 1275 512"><tr><th>Tens</th><th>Ones</th></tr><tr><td>    </td><td>..</td></tr><tr><td>    </td><td></td></tr><tr><td></td><td></td></tr></table> <p>When confident, children then use column addition to record.</p> <p>E.g. 28 + 7</p> $\begin{array}{r} 28 \\ 7 + \\ \hline 35 \end{array}$ | Tens | Ones |  | .. |  |  |  |  |
| Tens                                                                                                                                                    | Ones                                                                                                                                                                                                                                              |                                                                                                                                                                                                                                                                                                                                                                                                               |      |      |  |    |  |  |  |  |
|                                                                                                                                                         | ..                                                                                                                                                                                                                                                |                                                                                                                                                                                                                                                                                                                                                                                                               |      |      |  |    |  |  |  |  |
|                                                                                                                                                         |                                                                                                                                                                                                                                                   |                                                                                                                                                                                                                                                                                                                                                                                                               |      |      |  |    |  |  |  |  |
|                                                                                                                                                         |                                                                                                                                                                                                                                                   |                                                                                                                                                                                                                                                                                                                                                                                                               |      |      |  |    |  |  |  |  |

## Adding 2-digit number and ones

| Concrete                                                                                                                                                                                                                                                                                                                                                                       | Pictorial                                                                                                                                                                                                                                                                                 | Abstract                                                                                                                                     |
|--------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|----------------------------------------------------------------------------------------------------------------------------------------------|
| <p>Children must have a strong understanding of place value here. They must first know that 1 ten is the same as 10 ones.</p> <p>Tens frames and counters used to support bridging ten when adding.</p> <p>Use base ten and numicon to count on from larger number.</p> <p>E.g. 28 + 7</p>  | <p>Children use a marked number line to record this as jumps of one.</p> <p>They move on to an unmarked number line and use their knowledge of number bonds to bridge ten first.</p> <p>17 + 5 =</p>  | <p>When confident, children then use column addition to record.</p> <p>E.g. 28 + 7</p> $\begin{array}{r} 28 \\ 7 + \\ \hline 35 \end{array}$ |

## Add pairs of 2-digit numbers (including bridging 10)

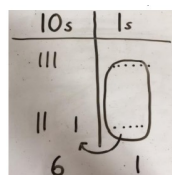
| Concrete                                                                                                                                                         | Pictorial                                                                                                                                         | Abstract                                                                                                                                                                                                     |
|------------------------------------------------------------------------------------------------------------------------------------------------------------------|---------------------------------------------------------------------------------------------------------------------------------------------------|--------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
|  <p>Use place value charts to place the base ten and then use jottings to</p> | <p>63 + 16</p>  <p>Use a number line to demonstra visually</p> | <p>Once children can add a multiple of ten to a 2-digit number mentally (e.g. 80+11) they are ready for adding pairs of 2-digit numbers that DO cross the tens boundary (e.g. 58 + 43).</p> $\underline{28}$ |

draw the tens and ones beneath the numbers.

$$35 + 26 =$$

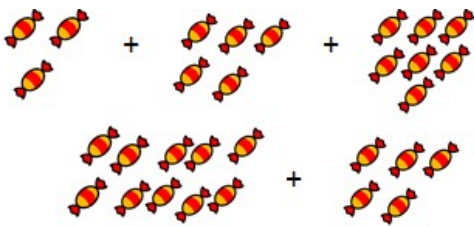
Partition both numbers, add together the ones. Have we got 10 ones? Exchange 10 ones for 1 ten. How many ones do we have? How many tens do we have?

Children to represent the base 10 in a place value chart.



$$\begin{array}{r} 17 + \\ 45 \\ \hline 1 \end{array}$$

## Adding 3 single digits

| Concrete                                                                                                                                                                                                                                                                       | Pictorial                                                                                                                                                                          | Abstract                                                                                                                                  |
|--------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|-------------------------------------------------------------------------------------------------------------------------------------------|
| <p><math>4 + 7 + 6 = 17</math><br/>Put 4 and 6 together to make 10. Add on 7.</p>  <p>Following on from making 10, make 10 with 2 of the digits (if possible) then add on the third digit</p> |  <p>Add together three groups of objects. Draw a picture to recombine the groups to make 10.</p> | <p><math>(4 + 7) + 6 = 10 + 7</math><br/><math>= 17</math></p> <p>Combine the two numbers that make 10 and then add on the remainder.</p> |

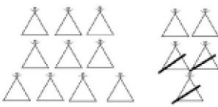
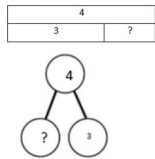
## Subtraction - Year 1

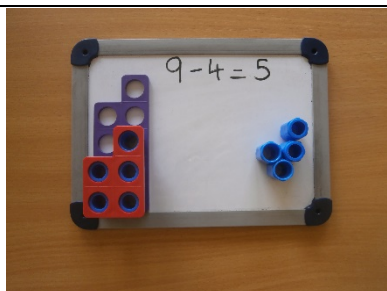
# Subtract from numbers up to 20

### Key number skills for subtraction at Year 1:

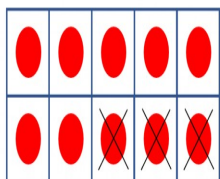
- Given a number, say one more or one less.
- Count to and over 100, forward and back, from any number.
- Represent and use subtraction facts to 20 and within 20.
- Subtract with one-digit and two-digit numbers to 20 including zero.
- Solve one-step problems that involve addition and subtraction, using concrete objects (i.e. Bead string, objects, cubes) and pictures and missing number problems.
- Read and write numbers from 0 to 20 in numerals and words.

### Subtracting by taking away ones (applicable up to 10)

| Concrete                                                                                        | Pictorial                                                                                                                                                                            | Abstract                                                                                                                                                                                                                                        |
|-------------------------------------------------------------------------------------------------|--------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| <p>Use physical objects, counters, cubes numicon etc to show how objects can be taken away.</p> | <p>Cross out drawn objects to show what has been taken away.</p>  <p><math>15 - 3 = 12</math></p> | <p>Look at how a part-whole model and bar model can be used to support understanding.</p> <p><math>4 - 3 =</math></p> <p><math>\square = 4 - 3</math></p>  |



$10 - 3 =$  Counting the number of counters on to the ten frame and then removing the counters to find the answer.



### Subtraction as breaking apart (applies within 10)

| Concrete                                                                                                                                                                                                                                                            | Pictorial                                                                                                                                                                                                  | Abstract                                                                               |
|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|----------------------------------------------------------------------------------------|
| <p>Building on their understanding of finding a part, they are introduced to subtraction by partitioning.</p> <p>Use cubes to build towers then break into parts.</p> <p>E.g <math>6 - 2</math></p> <p>Break 2 off</p> <p>What is left? What is the other part?</p> | <p>Use stories to find missing parts.</p> <p>How many ice creams do not have flakes?</p> <p>Draw pictures of this to support alongside tower of cubes.</p> <p>Represent this using a part-whole model.</p> | <p>Record as number sentence: <math>6 - 2 = 4</math></p> <p><math>4 = 6 - 2</math></p> |

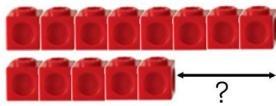
### Subtracting by counting back

| Concrete                                                                                                                                                                 | Pictorial                                          | Abstract                                                                                                                 |
|--------------------------------------------------------------------------------------------------------------------------------------------------------------------------|----------------------------------------------------|--------------------------------------------------------------------------------------------------------------------------|
| <p>Make the number in subtraction.</p> <p>larger your Move</p> <p>Use counters and move them away from the group as you take them away counting backwards as you go.</p> | <p>Count back on a number line or number track</p> | <p>Put 13 in your head, count back 4. What number are you at? Use your fingers to help. Record as a number sentence.</p> |

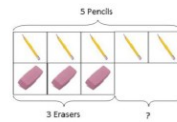
### Finding the difference

| Concrete | Pictorial | Abstract |
|----------|-----------|----------|
|----------|-----------|----------|

Compare amounts and objects to find the difference. Use cubes to build towers to find the difference.



Count on to find the difference.



Use basic bar models with items to find the difference.

Find the difference between 8 and 5.

8 - 5, the difference is

## Year 2

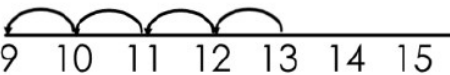
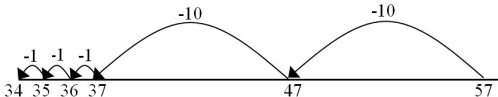
Subtract with 2-digit numbers

### Key number skills for subtraction Year 2:

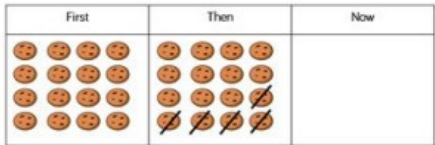
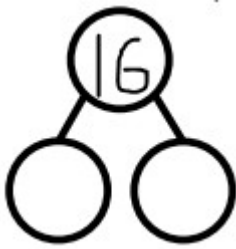
- Recognise the place value of each digit in a 2-digit number.
- Recall and use subtraction facts to 20 fluently and derive and use related facts up to 100.
- Subtract using concrete objects, pictorial representations, including a 2-digit number and units, a 2-digit number and tens and two 2-digit numbers.
- Show that subtraction cannot be done in any order.
- Read and write numbers to at least 100 in numerals and words.
- Solve simple addition and subtraction problems including measures, using concrete objects, pictorial representations and increasing confidence.
- Recognise and use inverse relationship between addition and subtraction, using this to check calculations and missing number problems.

**Note: Continue to refer to the part-whole model and bar model to record subtraction and to support the commutative law.**

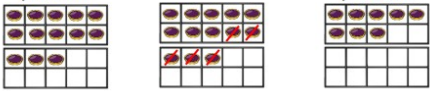
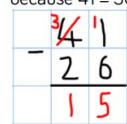
Subtraction – Counting back using a number line

| Concrete                                                                                                                                                                                                                                                                                                                      | Pictorial                                                                                                                                                                                                                                                                                                                                                                                                               | Abstract                                                                                                                 |
|-------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|--------------------------------------------------------------------------------------------------------------------------|
| <p>Make the number in subtraction. the beads your bead string as you count backwards in ones.</p>  <p>larger your Move along</p> <p>Use counters and move them away from the group as you take them away counting backwards as you go.</p> | <p>Count back on a number line or number track</p>  <p>Start at the bigger number and count back the smaller number showing the jumps on the number line.</p> <p>This can progress all the way to counting back using two 2-digit numbers.</p>  | <p>Put 13 in your head, count back 4. What number are you at? Use your fingers to help. Record as a number sentence.</p> |

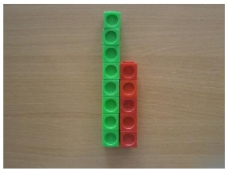
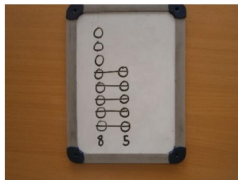
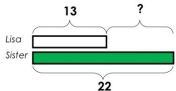
## Subtraction - not crossing 10

| Concrete                                                                                                                                                                                                                                                                                                                                                   | Pictorial                                                                                                                                                                                                                               | Abstract                                                                                                                                                                                                                                                                                                                  |
|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|-----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| <p>Build on language of subtraction within 20. Use of part-whole model key to reinforce number bonds within 20. Continue to subtract through stories (First, then, now)</p> <p>Use cubes, counters or other counting items to represent what is needed in the story.</p>  | <p>First there were ____ biscuits<br/>Then ____ were eaten.<br/>Now there are ____ biscuits.</p>  <p>Use part-whole model alongside manipulatives.</p> | <p><math>16 - 5 =</math></p> <p>Move on to number lines to jump back in preparation for crossing ten.</p>  <p>Most able and when appropriate to move to column subtraction.</p> $\begin{array}{r} 47 \\ - 13 \\ \hline 34 \end{array}$ |

## Subtraction - crossing 10

| Concrete                                                                                                                                                                                                                                                                                                                                                                                                                                                                          | Pictorial                                                                                                                                                                                                                                                                                                                        | Abstract                                                                                                                                                                                                                                                                                                                                                                                                     |
|-----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|--------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| <p>This small step focusses on the strategy of partitioning to make ten. Continue to use stories to support this step.</p> <p>First there were 13 jam tarts    Then 5 were eaten    Now there are 8 jam tarts.</p>  <p>Use ten frames to place counters to represent the numbers here.</p> <p><math>13 - 5</math><br/>First show <math>13 - 3 = 10</math><br/>Then <math>10 - 2 = 8</math></p> |  <p>Alongside the tens frames show this on a marked number line.</p> <p>Encourage children to partition the 1 digit number to see how to get to ten.</p> $\begin{array}{r} 13 - 5 \\ \phantom{13} \underline{3} \phantom{2} \\ 8 \end{array}$ | <p>Record as <math>13 - 5 = 8</math><br/>Can record steps after partitioning:<br/><math>13 - 5</math></p> <p><math>13 - 3 = 10</math><br/><math>10 - 2 = 8</math></p> <p>Formal column method. Children must understand that when they have exchanged the 10 they still have 41 because <math>41 = 30 + 11</math>.</p>  |

## Subtraction – Finding the Difference

| Concrete                                                                                                                                                                                 | Pictorial                                                                                                                                                                                                                                         | Abstract                                                                                                                                                                                                                       |
|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|--------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
|  <p>Compare objects and amounts to find the difference. Build towers to show the different amounts.</p> |  <p>Draw circles in rows then match. Shade on squared paper to show the two amounts. Count on a marked number line. Children jump along and count the jumps.</p> |  <p>Draw bars to find the difference. Jump back on a blank number line from one number to the other to see how much you have taken away</p> |

## Multiplication – Year 1

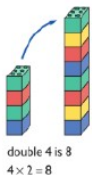
### Year 1

## Multiply with concrete objects, arrays and pictorial representations

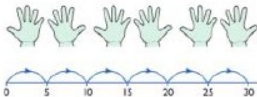
### Key number skills for multiplication at Year 1:

- Count in multiples of 2, 5 and 10.
- Solve one-step problems involving multiplication, by calculating the answer using concrete objects, pictorial representations and arrays with the support of the teacher.
- Make connections between arrays, number patterns, and counting in twos, fives and tens.
- Begin to understand doubling using concrete objects and pictorial representations.

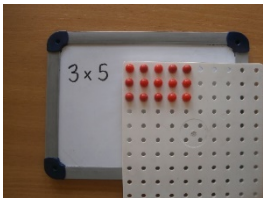
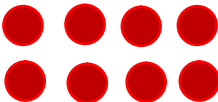
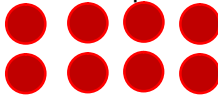
### Doubling

| Concrete                                                                                                                                            | Pictorial                                                                                                                                                     | Abstract |
|-----------------------------------------------------------------------------------------------------------------------------------------------------|---------------------------------------------------------------------------------------------------------------------------------------------------------------|----------|
| <p>Use practical activities to show how to double a number.</p>  | <p>Draw pictures to show how to double a number.</p> <p>Double 4 is 8</p>  |          |

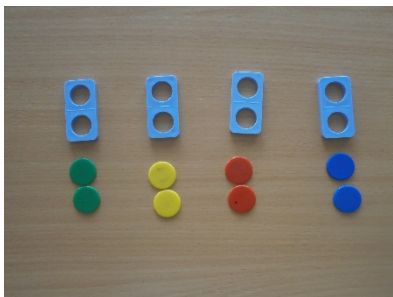
## Counting in multiples

| Concrete                                                                                                                                                   | Pictorial                                                                                                                                                            | Abstract                                                                                                                                          |
|------------------------------------------------------------------------------------------------------------------------------------------------------------|----------------------------------------------------------------------------------------------------------------------------------------------------------------------|---------------------------------------------------------------------------------------------------------------------------------------------------|
| <p>Count in multiples supported by concrete objects in equal groups.</p>  | <p>Use a number line or pictures to continue support in counting in multiples.</p>  | <p>Count in multiples of a number aloud.</p> <p>Write sequences with multiples of numbers.</p> <p>2, 4, 6, 8, 10</p> <p>5, 10, 15, 20, 25, 30</p> |

## Using Arrays to solve multiplication

| Concrete                                                                                                                                                                            | Pictorial                                                                                                                                                                              | Abstract                                                                                                                                                                                                                                                                                                       |
|-------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| <p>Create arrays using pegs and boards, cubes and counters to show multiplication sentences.</p>  | <p>Draw arrays for multiplication sentences.</p>  <p>2 rows of 4<br/> <math>2 \times 4 = 8</math></p> | <p>Use an array to write multiplication sentences and reinforce repeated addition.</p>  <p><math>4 + 4 = 8</math><br/> <math>2 + 2 + 2 + 2 = 8</math><br/> <math>2 \times 4 = 8</math><br/> <math>4 \times 2 = 8</math></p> |

## Repeated Addition

| Concrete                                                                                                                                                                            | Pictorial                                                                                                                         | Abstract                                                                                                                                                                                                                                                                                                |
|-------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|-----------------------------------------------------------------------------------------------------------------------------------|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| <p>Use counting equipment and numicon to find groups of the same number by adding together.</p>  | <p>Draw counters in sets to add together.</p>  | <p>Write addition sentences to describe objects and pictures.</p>  <p><math>2 + 2 + 2 + 2 + 2 = 10</math></p> <p><math>2 + 2 + 2 + 2 + 2 = 10</math></p> <p>Jump along a marked number line in repeated jumps.</p> |

## Year 2

### Multiply using arrays and repeated addition (using at least 2s, 5s and 10s)

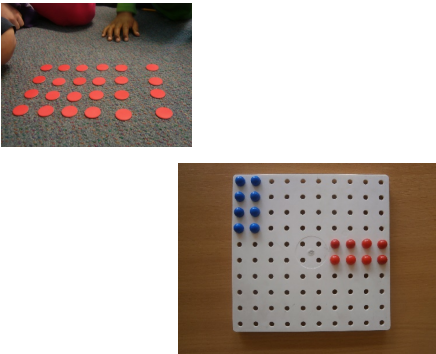
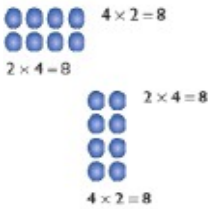
#### Key number skills for multiplication at Year 2:

- Count in steps of 2, 3 and 5 from zero, and in 10s from any number.

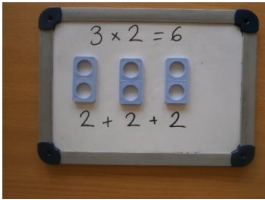
- Recall and use multiplication facts from the 2, 5 and 10 multiplication tables, including recognising odds and evens.
- Write and calculate number sentences using the x and = signs.
- Show that multiplication can be done in any order (commutative).
- Solve a range of problems involving multiplication, using concrete objects, arrays, repeated addition, mental methods, and multiplication facts.
- Pupils use a variety of language to discuss and describe multiplication.

**Note: Continue to refer to the part-whole model to support the commutative law.**

### Arrays showing commutative multiplication (gives the same result whatever the order of the digits)

| Concrete                                                                                                                                                                             | Pictorial                                                                                                                                                                        | Abstract                                                                                                                                                                                                                                                                                                                     |
|--------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| <p>Create arrays using pegs and boards, cubes and counters to show multiplication sentences..</p>  | <p>Draw arrays in different rotations to find <b>commutative</b> multiplication sentences.</p>  | <p>Use an array to write multiplication sentences and reinforce repeated addition.</p>  <p> <math>5 + 5 + 5 = 15</math><br/> <math>3 + 3 + 3 + 3 + 3 = 15</math><br/> <math>3 \times 5 = 15</math><br/> <math>5 \times 3 = 15</math> </p> |

### Repeated Addition

| Concrete                                                                                                                                                                                                         | Pictorial                                                                                                                                                                                                                     | Abstract                                                                                                                                              |
|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|-------------------------------------------------------------------------------------------------------------------------------------------------------|
| <p>See multiplication as 'groups of' or 'lots of' by collecting group of an amount using numicon and counting equipment.</p>  | <p>Draw counters in sets to add together. Record as repeated addition. <math>2 + 2 + 2 = 6</math> Show jumps on a marked number line.</p>  | <p>Record as repeated addition<br/> <math>2 + 2 + 2 = 6</math><br/> <math>3 \times 2 = 6</math><br/>           Show jumps on a blank number line.</p> |

### Use mental recall

Children should begin to recall multiplication facts for 2, 5 and 10 times tables through practice in counting and understanding of the operation.

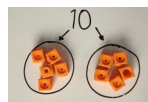
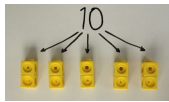
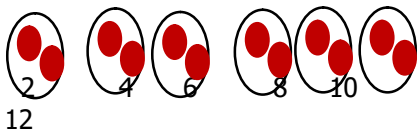
# Group and share small quantities

Key number skills needed for division at Year1:

- Solve one-step problems involving multiplication and division, by calculating the answer using concrete objects, pictorial representations, arrays with the support of the teacher.
- Through grouping and sharing small quantities, pupils begin to understand division and finding simple fractions of objects, numbers and quantities.
- They make connections between arrays, number patterns, and counting in twos, fives and tens.

**Note: Continue to refer to the part-whole model and bar model to support the commutative law.**

## Division as grouping

| Concrete                                                                                                                                                                                                                                                                                                        | Pictorial                                                                                                                                                                                                               | Abstract                                  |
|-----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|-------------------------------------------|
| <p>Use everyday items and counting equipment to share between groups. E.g I have 10 cubes, can you share them equally in 2 groups?.</p>   | <p>Children use pictures or draw counters to share quantities.</p>                                                                  | <p>Share 9 buns between three people.</p> |
| Concrete                                                                                                                                                                                                                                                                                                        | Pictorial                                                                                                                                                                                                               | Abstract                                  |
| <p>Divide quantities into equal groups. Use cubes, counters, objects or place value counters to aid understanding.</p>                    | <p>Use jottings for groupings.</p> <p>E.g. How many equal groups of 2 are in 12? Draw groups of 2 until they have 12 in total.</p>  |                                           |

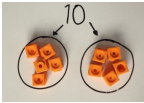
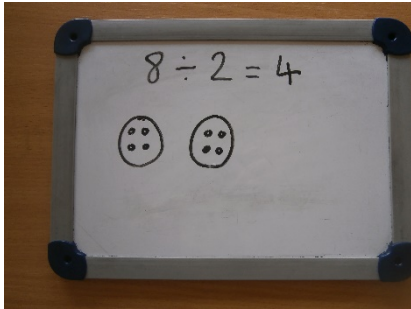
## Division -Year 2

### Group and share using the $\div$ and $=$ sign

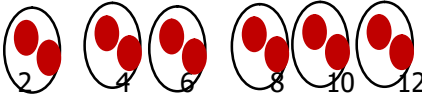
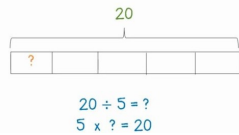
#### Key number skills needed for division at Year 2:

- Count in steps of 2, 3, and 5 from 0.
- Recall and use multiplication and division facts for the 2, 5 and 10 multiplication tables, including recognising odd and even numbers.
- Calculate mathematical sentences for multiplication and division within the multiplication tables and write them using the  $\times$ ,  $\div$  and  $=$  signs.
- Show that multiplication of two numbers can be done in any order (commutative) and division of one number by another cannot.
- Solve problems involving multiplication and division, using materials, arrays, repeated addition, mental methods, and multiplication and division facts, including problems in contexts.

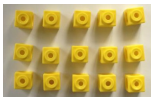
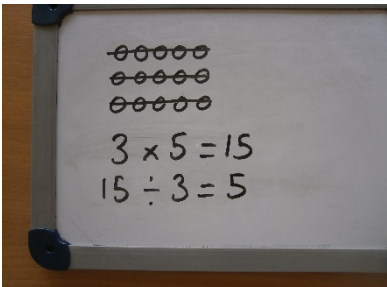
#### Division as sharing

| Concrete                                                                                                                                                                                                   | Pictorial                                                                                                                                                                                          | Abstract                                                                                    |
|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|---------------------------------------------------------------------------------------------|
| <p>Divide quantities into equal groups. Use cubes, counters, objects or place value counters to aid understanding.</p>  | <p>Draw circles and share by drawing counters inside these one at a time. A bar model could also be used.</p>  | <p>Divide 28 into 2 groups. How many are in each group?</p> <p><math>28 \div 2 =</math></p> |

#### Division as grouping

| Concrete                                                                                                                                                                                                                              | Pictorial                                                                                                                                                                                                               | Abstract                                                                                                                                                             |
|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|----------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| <p>Children use concrete manipulatives to group in a variety of ways.</p> <p>E.g. there are 6 sweets, how many people can have 2 sweets each?</p>  | <p>Use jottings for groupings.</p> <p>E.g. How many equal groups of 2 are in 12? Draw groups of 2 until they have 12 in total.</p>  | <p>Show on a bar model and refer to inverse relationship – multiplication.</p>  |

## Division within arrays

| Concrete                                                                                                                                                                                                                                                                                                                                            | Pictorial                                                                                                                                                                                           | Abstract                                                                                                                                                                                                                                          |
|-----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|-----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
|  <p>Link division to multiplication by creating an array and thinking about the number sentences that can be created.</p> <p>Eg <math>15 \div 3 = 5</math>      <math>5 \times 3 = 15</math><br/> <math>15 \div 5 = 3</math>      <math>3 \times 5 = 15</math></p> | <p>Draw an array and use lines to split the array into groups to make multiplication and division sentences.</p>  | <p>Find the inverse of multiplication and division sentences by creating four linking number sentences.</p> <p><math>3 \times 5 = 15</math><br/> <math>5 \times 3 = 15</math><br/> <math>15 \div 3 = 5</math><br/> <math>15 \div 5 = 3</math></p> |